

# *TMDD Model Translated from NONMEM (NM-TRAN) to Phoenix NLME (PML)*

Phoenix Modeling Language School

March 22, 2018

Loan Pham, Ph.D.

Senior Pharmacokinetic Scientist

Camargo Pharmaceutical Services

9825 Kenwood Road, Suite 203

Cincinnati, OH 45242

# Agenda

- TMDD Model: Brief Overview
- 1 compartment, A Single Dose IV Bolus Example:
  - ✓ NONMEM versus PHOENIX NLME
- Demonstration
- Questions and Answers

# TMDD Model Selected Publications: Model Development and Applications

1. Mager, D.E. and Jusko, W.J. General pharmacokinetic model for drugs exhibiting target mediated drug disposition. J Pharmacokinet Pharmacodyn 28 (2001):507–32.
2. Mager, D.E. and Krzyzanski, W. Quasi-equilibrium pharmacokinetic model for drugs exhibiting target-mediated drug disposition. Pharm Res 22 (2005):1589–96.
3. **Gibiansky, L., Gibiansky, E.**, Kakkar, T. and Ma, P. Approximations of the target mediated drug disposition model and identifiability of model parameters. J Pharmacokinet Pharmacodyn 35 (2008):573–91.A\*
4. **Gibiansky, L. and Gibiansky, E.** Target-mediated drug disposition model: approximations, identifiability of model parameters and applications to the population pharmacokinetic-pharmacodynamic modeling of biologics. Expert Opin Drug Metab Toxicol 5 (2009):803–12.\*
5. Yan, X., Mager, D.E. and Krzyzanski, W. Selection between michaelis-menten and target-mediated drug disposition pharmacokinetic models. J Pharmacokinet Pharmacodyn 37 (2010):25–47.

# TMDD Model Selected Publications (continued)

6. P Dua, E Hawkins, PH van der Graaf. A Tutorial on Target-Mediated Drug Disposition (TMDD) Models CPT Pharmacometrics Syst Pharmacol. 2015 Jun; 4(6): 324–337. Published online 2015 Jun 15. doi: 10.1002/psp4.41 PMCID: PMC4505827

7. **Lambertus A. Peletier, Johan Gabrielsson** Dynamics of target-mediated drug disposition: characteristic profiles and parameter identification. J Pharmacokinet Pharmacodyn. 2012 Oct; 39(5): 429–451. Published online 2012 Aug 1. doi: 10.1007/s10928-012-9260-6 PMCID: PMC3446204

## Additional Background on TMDD Model – Assumptions and Challenges:

- PML School: Target-mediated Drug Disposition (TMDD) Modeling Using the Quasi-equilibrium Assumption 30-NOV-2017 Frank Striebel – MorphoSys AG
- PML school lesson 6 : full TMDD model
- Metrum MI 212, lecture 4 and lab 4\*

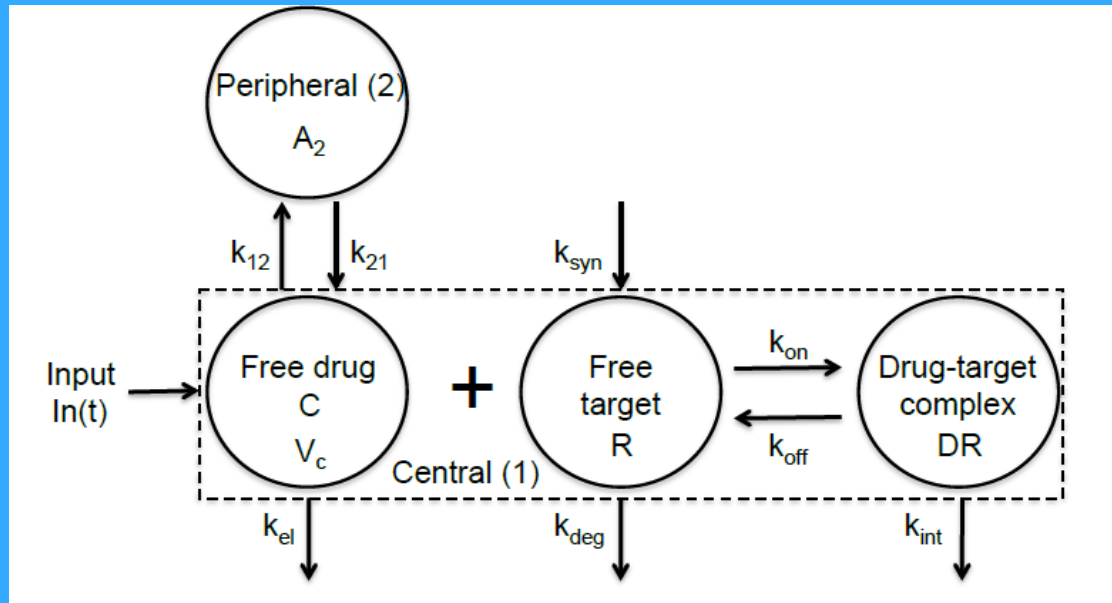
# Exhibited TMDD Drugs

**Table 1** Examples of the ligands and receptors exhibiting TMDD that have been modeled in the current literature

| Ligand                  | Receptor         | PK model used                               | PD model used | Biomarker                      | Reference |
|-------------------------|------------------|---------------------------------------------|---------------|--------------------------------|-----------|
| Gemtuzumab ozogamicin   | CD33 antigen     | One Compartment Cell Level Kinetic          | No            | N/A                            | 31        |
| Type 1 IFN              | IFNAR1 or IFNAR2 | Two Compartment Ctot and Rtot               | No            | N/A                            | 41        |
| Canakinumab             | IL-1 $\beta$     | Binding in Two Compartments QSS             | No            | N/A                            | 60        |
| Canakinumab             | IL-1 $\beta$     | Binding in Two Compartments                 | Yes           | CRP and SAA                    | 62        |
| Tocilizumab             | IL-6R (soluble)  | Two Compartment QSS with MM elimination     | Yes           | Neutrophil, platelets          | 64        |
| rhLIF                   | LIF receptor     | Two Compartment with 2 Depots               | No            | N/A                            | 73        |
| Anti-MTX mAb            | MTX              | Two Compartment                             | No            | N/A                            | 65        |
| Denosumab               | RANKL            | One Compartment QE with constant Rtot       | Yes           | Serum NTX                      | 71        |
| Denosumab               | RANKL            | Two Compartment QSS with Depot              | No            | N/A                            | 63        |
| PEG-TPOm                | TPO              | One Compartment                             | Yes           | Platelets from precursor cells | 56        |
| Infliximab              | TNF $\alpha$     | One Compartment with Depot                  | No            | N/A                            | 53        |
| Aflibercept (VEGF-Trap) | VEGF             | Two Compartment MM                          | No            | N/A                            | 67        |
| rhVEGF                  | VEGF receptors   | Two Compartment with constant R             | No            | N/A                            | 77        |
| Filgrastim              | G-CSF receptor   | One Compartment with Depot                  | No            | N/A                            | 78        |
| Anti-CD81 mAb           | CD81             | One Compartment QE                          | No            | N/A                            | 80        |
| TAM-163                 | TrkB             | Two Compartment with Depot                  | No            | N/A                            | 81        |
| HSP90 Inhibitors        | HSP90            | Both Two Compartment and One Compartment RB | No            | N/A                            | 82        |
| AMG-811                 | IFN- $\gamma$    | One Compartment QSS                         | No            | N/A                            | 44        |

Reproduced from Dua et al, *A Tutorial on Target-Mediated Drug Disposition (TMDD) Models* 2015CPT Pharmacometrics Syst. Pharmacol. (2015) 4, 324–337

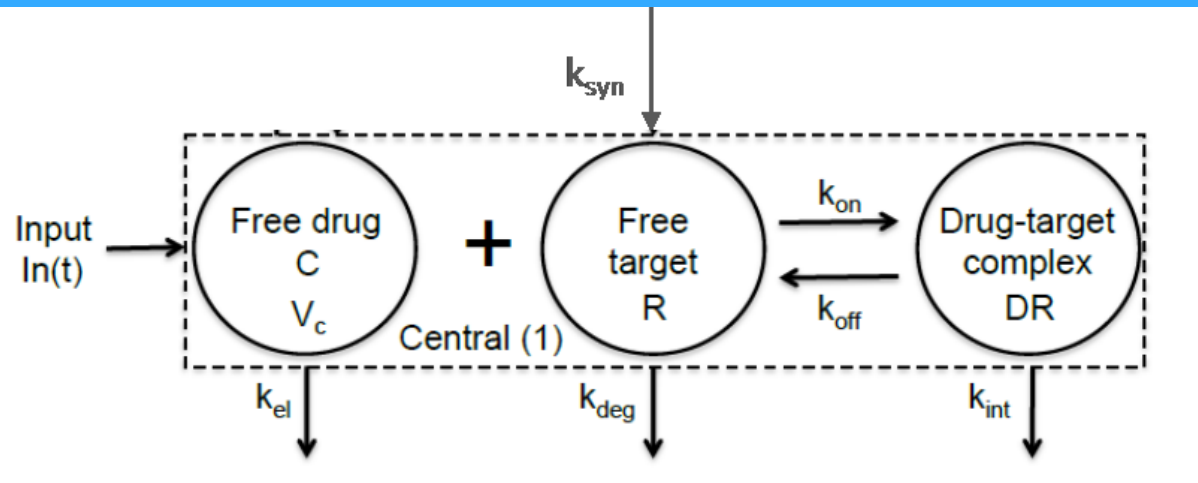
# TMDD 2 Compartmental Model Overview



*Reproduced from Mager DE and Krzyzanski W, 2005*

- $C$ ,  $R$ ,  $DR$  (RC): Molar concentrations of free (unbound) drug, free target, and drug-target complex in the central compartment, respectively
- $A_a$ : amount of drug (moles) in the peripheral compartment
- $In(t)$  is a function of drug input or endogenous substance production
- $V_c$  (V) is the central compartment volume
- $k_{el}$ ,  $k_{12}$ , and  $k_{21}$  are the linear elimination, central to peripheral, and peripheral to central rate constants, respectively, for the drug
- $k_{syn}$  and  $k_{deg}$  are the target synthesis and degradation rate constants, respectively
- $k_{on}$  and  $k_{off}$  are the binding and dissociation rate constants, respectively
- $k_{int}$  is the elimination rate constant for the drug-target complex

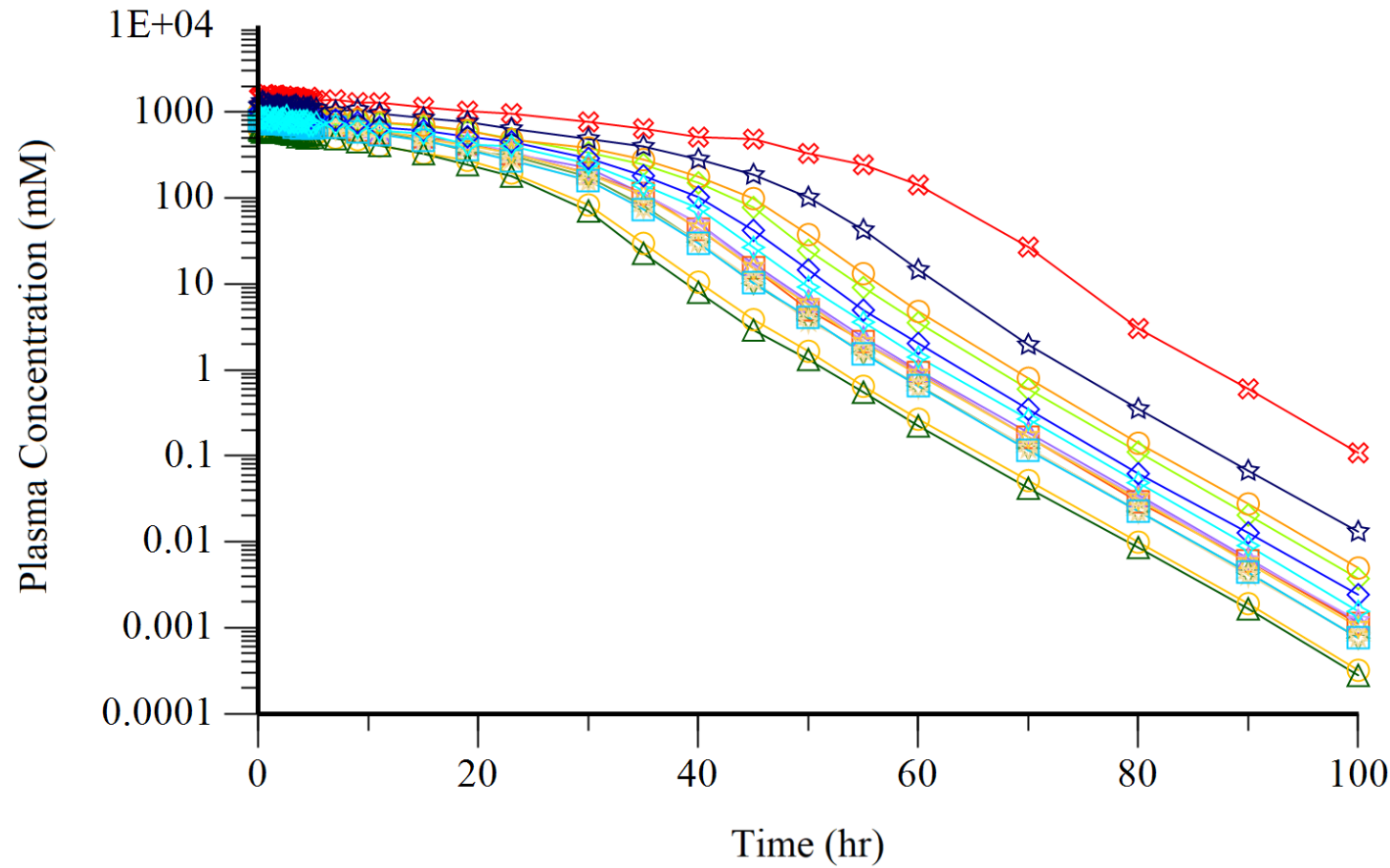
# TMDD 1 Compartmental Model Overview



*Reproduced from Mager DE and Krzyzanski W, 2005*

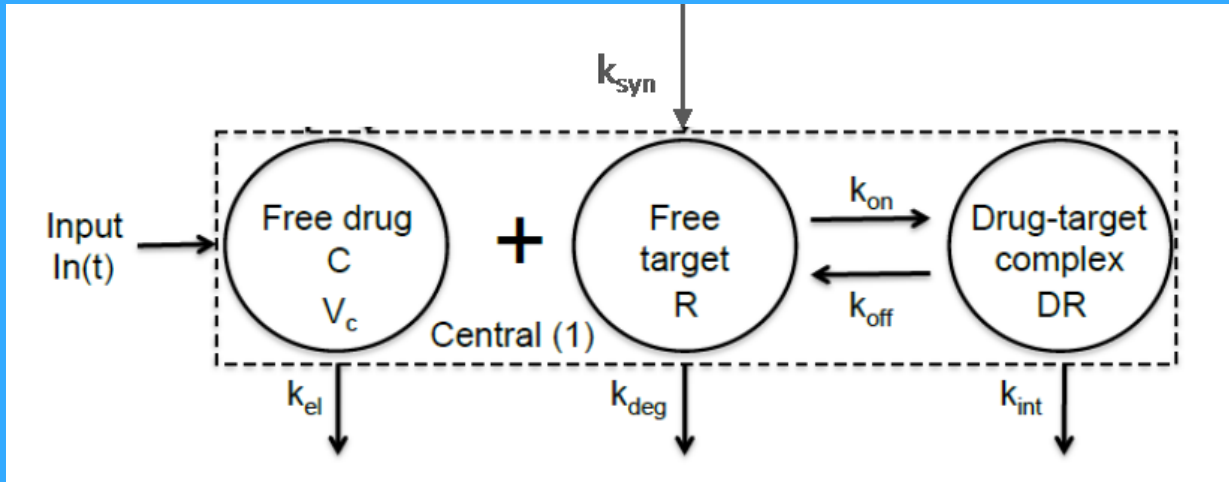
- $C$ ,  $R$ ,  $DR$  (RC): Molar concentrations of free (unbound) drug, free target, and drug-target complex in the central compartment, respectively
- $A_a$ : amount of drug (moles) in the peripheral compartment
- $In(t)$  is a function of drug input or endogenous substance production
- $V_c$  ( $V$ ) is the central compartment volume
- $k_{el}$  is the linear elimination rate constant, respectively, for the drug
- $k_{syn}$  and  $k_{deg}$  are the target synthesis and degradation rate constants, respectively
- $k_{on}$  and  $k_{off}$  are the binding and dissociation rate constants, respectively
- $k_{int}$  is the elimination rate constant for the drug-target complex

# TMDD Model: Example



- A single dose intravenous bolus administration: 1000 unit dose
- 15 subjects
- 100 hr sampling time points
- Only individual drug plasma concentration vs. time profiles are available

# TMDD with QE Approximation- 1 Compartmental Model



## Assumptions:

$$k_{on} C \cdot R - k_{off} RC = 0;$$

$$\frac{C \cdot R}{RC} = \frac{k_{off}}{k_{on}} = K_D,$$

- $K_d$ : equilibrium dissociation constant
- $C_{tot}$  and  $R_{tot}$ : total (free and bound) concentration of the drug in the central compartment and the total concentration of the Receptor
- $C_{tot} = C + RC$
- $R_{tot} = R + RC$

$$C = \frac{1}{2} \left[ (C_{tot} - R_{tot} - K_D) + \sqrt{(C_{tot} - R_{tot} - K_D)^2 + 4K_D C_{tot}} \right]$$

$$RC = \frac{R_{tot} C}{K_D + C},$$

*Gibiansky, L., Gibiansky, E., Kakkar, T. and Ma, P. Approximations of the target mediated drug disposition model and identifiability of model parameters. J Pharmacokinet Pharmacodyn 35 (2008):573–91.A\**

# NLME Code: TMDD\_QE Approximation; 1 Compartment

| Derivative Equations                                                                                                                                                                                                                                                                                                                                                                                                                                                | Phoenix NLME                                                                                                                                                                                                                                                                                                                                                           |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>#Total drug concentration</p> $D\text{Ctot}/dt = \text{Dose} - k_{\text{int}} * \text{Ctot} - (k_{\text{el}} - k_{\text{int}}) * C$ <p>; (modified Eq14)</p> $\text{Ctot} = \text{Atot}/V$<br>$K_D = k_{\text{off}}/k_{\text{on}}$ <p>#Free drug in central compartment</p> $C = 1/2 * ((\text{Ctot} - \text{Rtot} - K_D) + \sqrt{(\text{Ctot} - \text{Rtot} - K_D)^2 + 4 * K_D * \text{Ctot}})$<br>$RC = \text{Rtot} * C / (K_D + C)$<br>$R = \text{Rtot} - RC$ | $\text{deriv}(\text{Atot} = - k_{\text{int}} * V * \text{Ctot} - (k_{\text{el}} - k_{\text{int}}) * C * V)$ $\text{Ctot} = \text{Atot}/V$<br>$K_D = k_{\text{off}}/k_{\text{on}}$ $C = 1/2 * ((\text{Ctot} - \text{Rtot} - K_D) + \sqrt{(\text{Ctot} - \text{Rtot} - K_D)^2 + 4 * K_D * \text{Ctot}})$<br>$RC = \text{Rtot} * C / (K_D + C)$<br>$R = \text{Rtot} - RC$ |

*Gibiansky, L., Gibiansky, E., Kakkar, T. and Ma, P. Approximations of the target mediated drug disposition model and identifiability of model parameters. J Pharmacokinet Pharmacodyn 35 (2008):573–91.A\**

# DATASET COMPARISON: NONMEM vs Phoenix NLME

NONMEM → Phoenix NLME

| 1  | ID | GROUP | TIME  | AMT  | DV      | RCCOM   | EVID | CMT |
|----|----|-------|-------|------|---------|---------|------|-----|
| 2  | 15 | 1000  | 0     | 1000 | .       | .       | 1    | 1   |
| 3  | 15 | 1000  | 0.083 | .    | 620.125 | 97.1072 | 0    | 1   |
| 4  | 15 | 1000  | 0.17  | .    | 678.832 | 97.022  | 0    | 1   |
| 5  | 15 | 1000  | 0.34  | .    | 721.162 | 97.2952 | 0    | 1   |
| 6  | 15 | 1000  | 0.51  | .    | 653.176 | 97.9945 | 0    | 1   |
| 7  | 15 | 1000  | 0.68  | .    | 622.716 | 95.8917 | 0    | 1   |
| 8  | 15 | 1000  | 0.85  | .    | 639.29  | 96.6203 | 0    | 1   |
| 9  | 15 | 1000  | 1.02  | .    | 627.767 | 96.595  | 0    | 1   |
| 10 | 15 | 1000  | 1.19  | .    | 640.363 | 96.7894 | 0    | 1   |
| 11 | 15 | 1000  | 1.36  | .    | 604.657 | 95.156  | 0    | 1   |
| 12 | 15 | 1000  | 1.53  | .    | 630.046 | 96.7902 | 0    | 1   |
| 13 | 15 | 1000  | 1.7   | .    | 609.257 | 96.7488 | 0    | 1   |
| 14 | 15 | 1000  | 1.87  | .    | 683.129 | 96.1019 | 0    | 1   |
| 15 | 15 | 1000  | 2.04  | .    | 587.367 | 96.5451 | 0    | 1   |
| 16 | 15 | 1000  | 2.21  | .    | 596.947 | 97.0301 | 0    | 1   |
| 17 | 15 | 1000  | 2.38  | .    | 601.644 | 95.8112 | 0    | 1   |
| 18 | 15 | 1000  | 2.55  | .    | 633.344 | 95.1978 | 0    | 1   |
| 19 | 15 | 1000  | 2.72  | .    | 594.672 | 98.787  | 0    | 1   |
| 20 | 15 | 1000  | 2.89  | .    | 596.945 | 96.6141 | 0    | 1   |
| 21 | 15 | 1000  | 3.06  | .    | 557.761 | 96.1893 | 0    | 1   |
| 22 | 15 | 1000  | 3.23  | .    | 596.611 | 97.2165 | 0    | 1   |
| 23 | 15 | 1000  | 3.4   | .    | 608.57  | 96.9831 | 0    | 1   |
| 24 | 15 | 1000  | 3.57  | .    | 596.294 | 97.2227 | 0    | 1   |
| 25 | 15 | 1000  | 3.74  | .    | 566.753 | 96.4092 | 0    | 1   |
| 26 | 15 | 1000  | 3.91  | .    | 567.779 | 98.1996 | 0    | 1   |
| 27 | 15 | 1000  | 4.08  | .    | 571.532 | 96.0171 | 0    | 1   |
| 28 | 15 | 1000  | 4.25  | .    | 576.881 | 96.164  | 0    | 1   |
| 29 | 15 | 1000  | 4.42  | .    | 545.807 | 96.2196 | 0    | 1   |
| 30 | 15 | 1000  | 4.59  | .    | 565.442 | 95.2916 | 0    | 1   |

SetupResultsVerification

Main (Dataset\_iv bolus\_...)

Model

DosingParametersParameters.MappingRandom Effects

Use Internal Worksheet

Rebuild

View Sou

|    | ID | Atot | Time |
|----|----|------|------|
| 1  | 15 | 1000 | 0    |
| 2  | 16 | 1000 | 0    |
| 3  | 17 | 1000 | 0    |
| 4  | 18 | 1000 | 0    |
| 5  | 19 | 1000 | 0    |
| 6  | 20 | 1000 | 0    |
| 7  | 21 | 1000 | 0    |
| 8  | 22 | 1000 | 0    |
| 9  | 23 | 1000 | 0    |
| 10 | 24 | 1000 | 0    |
| 11 | 25 | 1000 | 0    |
| 12 | 26 | 1000 | 0    |
| 13 | 27 | 1000 | 0    |
| 14 | 28 | 1000 | 0    |
| 15 | 29 | 1000 | 0    |
| *  |    |      |      |

Populati

GeneralParametersInput OptionsInitial Estimates

☐ Res

Note: Reset will not apply if run option 'Sort Input' is checked.

☐ MD

☐ Steady

☐ ADDL

☐ Dat

Edit text-mode infusion

Atot

dspt ☐ Infusio

|    | ID | dose | time  | Cfree   |
|----|----|------|-------|---------|
| 1  | 15 | 1000 | 0.083 | 620.125 |
| 2  | 15 | 1000 | 0.17  | 678.832 |
| 3  | 15 | 1000 | 0.34  | 721.162 |
| 4  | 15 | 1000 | 0.51  | 653.176 |
| 5  | 15 | 1000 | 0.68  | 622.716 |
| 6  | 15 | 1000 | 0.85  | 639.29  |
| 7  | 15 | 1000 | 1.02  | 627.767 |
| 8  | 15 | 1000 | 1.19  | 640.363 |
| 9  | 15 | 1000 | 1.36  | 604.657 |
| 10 | 15 | 1000 | 1.53  | 630.046 |
| 11 | 15 | 1000 | 1.7   | 609.257 |
| 12 | 15 | 1000 | 1.87  | 683.129 |
| 13 | 15 | 1000 | 2.04  | 587.367 |
| 14 | 15 | 1000 | 2.21  | 596.947 |
| 15 | 15 | 1000 | 2.38  | 601.644 |
| 16 | 15 | 1000 | 2.55  | 633.344 |
| 17 | 15 | 1000 | 2.72  | 594.672 |
| 18 | 15 | 1000 | 2.89  | 596.945 |
| 19 | 15 | 1000 | 3.06  | 557.761 |

# TMDD\_QE NONMEM vs. Phoenix NLME

```
$PROB TMDD_QE DATA
$INPUT ID GROUP TIME AMT DV RCCOM EVID CMT
$DATA DATA1000.csv IGNORE=C
$SUBROUTINE ADVAN6 TOL = 6
$MODEL
COMP(1) ; 1 CMT

$PK
KEL = THETA(1)*EXP(ETA(1)) ; KEL for free drug
V1  = THETA(2)*EXP(ETA(2)) ; V1 for free drug
RTOT = THETA(3) ; total of free receptor
KON = THETA(4) ; binding rate constant
KOFF = THETA(5) ; dissociation rate constant
KINT = THETA(6) ; elimination rate constant for drug-receptor
complex
```

```
test(){
dosepoint(Atot); dose in 1000 mM, IV bolus; Volume in L, time
in hr

#The posthoc parameters are defined in the form of PML in
stparm statements. tvKel and tvV are fixed effects, and nKel and
nV are random effects
stparm(kel = tvkel*exp(nKel))
stparm(V = tvV*exp(nV))
stparm(Rtot = tvRtot)
stparm(kon = tvkon)
stparm(koff = tvkoff)
stparm(kint = tvkint)
```

# TMDD\_QE NONMEM vs Phoenix NLME

#Adapted from Gibiansky et al. 2008 Journal of Pharmacokinetics and Pharmacodynamics".

## \$DES

*; Adapted from Gibiansky et al. 2008 Journal of Pharmacokinetics and Pharmacodynamics*

DADT(1) = - KINT\*A(1) - (KEL - KINT)\*CFREE\*V1; C1 or Ctotal;

C1 = A(1)/V1 ;

KD = KOFF/KON ;

CFREE = 1/2\*((C1 - RTOT - KD) + SQRT((C1 - RTOT - KD)\*\*2 + 4\*KD\*C1)) ;

RC = RTOT\*CFREE/(KD + CFREE) ;

RFREE = RTOT - RC ;

# DE for the total drug amount in central compartment

deriv(Atot = - kint\*V\*Ctot - (kel - kint)\*C\*V)

#Total drug concentration

Ctot = Atot/V

#equilibrium dissociation constant

KD = koff/kon

#free drug concentration in central compartment

C = 1/2\*((Ctot-Rtot-KD)+sqrt((Ctot-Rtot-KD)^2+4\*KD\*Ctot))

#complex concentration

RC = Rtot\*C/(KD + C)

#free receptor concentration

R = Rtot - RC

# TMDD\_QE NONMEM vs Phoenix NLME

## \$THETA

(0, 0.005) ; 1 KEL  
(0, 1) ; 2 V1  
(100 FIXED) ; 3 RTOT  
(0.1 FIXED) ; 4 KON  
(0, 3) ; 5 KOFF  
(0, 0.2) ; 6 KINT

## \$ERROR

CALLFL=0; Call with every observation record  
KD2 = KOFF/KON; redefine Kd  
IPRED= 1/2\*((A(1)/V1 - RTOT - KD2) + SQRT((A(1)/V1 - RTOT - KD2)\*\*2 + 4\*KD2\*A(1)/V1)); redefine CFree;  
**Y=IPRED\*(1 + EPS(1));** individual predicted value in model  
IRES = DV - IPRED; individual residual observed-predicted  
IWRES = IRES/SQRT(IPRED\*\*2\*SIGMA(1,1)); proportional error model

#Fixed effects; initial estimate; parameters to be estimated#

fixef(tvkel= c(, 0.006, ))  
fixef(tvV = c(, 1, ))  
fixef(tvRtot = c(, 100,))  
fixef(tvkon = c(, 0.1, ))  
fixef(tvkoff = c(, 3, ))  
fixef(tvkint = c(,0.3,))

observe(CObs = C\*(1 + eps1)) # free drug in central compartment; multiplicative error model

}

# TMDD\_QE NONMEM vs Phoenix NLME

\$OMEGA

0.02 0.02 ; BSV KEL AND V1

\$SIGMA

0.02 ; variance of epsilon one

\$ESTIMATION METHOD=1 INTER NOABORT

MAXEVAL=999999 PRINT=10 ; FOCE

NSIG = 4 SIGL = 6

\$COV SIGL = 6 TOL = 6

\$TABLE ID TIME DV PRED IPRED RES IRES WRES

IWRES CWRES NOAPPEND NOPRINT ONEHEADER

FILE = SDTAB

\$TABLE ID KEL V1 RTOT KON KOFF KINT ETA1 ETA2

NOAPPEND NOPRINT ONEHEADER FIRSTONLY FILE =

PATAB

#random effect; within subject variability

ranef(diag(nV,nKel)=c(0.02,0.02))

#Initial estimate of the standard deviation for the residual error#

error(eps1 = 0.1414) ;

Demo

# Summary

- Set up and run NONMEM and PHOENIX NLME Model:
  - Population PK Modeling for TMDD\_QE Approximation
  - Single Dose IV Bolus Injection; 15 Subjects
- FOCE Interaction vs. FOCE ELS
- Similar Results Between NONMEM and PHOENIX NLME Model

Questions?



# Schedule for Q2

| Date   | Series        | Topic                                                                 |
|--------|---------------|-----------------------------------------------------------------------|
| 19-Apr | NONMEM-2-NLME | Nonlinear Elimination and Model Validation I: Bootstrap               |
| 3-May  | NONMEM-2-NLME | Mixed Absorption and Model Validation II: VPC                         |
| 17-May | NONMEM-2-NLME | Running NONMEM and Phoenix NLME in the Cloud                          |
| 31-May | NONMEM-2-NLME | PD Emax inhibitory with baseline and shape factor                     |
| 14-Jun | NONMEM-2-NLME | PD Indirect Response with IV Bolus Dosing                             |
| 28-Jun | NONMEM-2-NLME | PKPD 1 Compartment-IV Infusion - Emax with Baseline, Shape and Effect |

# Coming up...



## NONMEM-2-NLME

Nonlinear elimination and model validation I: Bootstrap

April 19, 2018 | 10am EST

*Presenter: Bernd Wendt*